

# The Role of Baseband Noise and Its Upconversion in HBT Oscillator Phase Noise

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**Abstract**—The phase noise spectral density ( $\mathcal{L}(f_m)$ ) of an 11.02-GHz heterojunction bipolar transistor (HBT) dielectric resonator oscillator (DRO) has been investigated in terms of the HBT's low frequency noise and the oscillator's upconversion coefficient. Experimental studies have been used for this purpose and the measured  $\mathcal{L}(f_m)$  ranged from  $-89$  dBc/Hz to  $-101$  dBc/Hz at a 10-kHz offset frequency (best phase noise spectral density performance was  $-124$  dBc/Hz at 100 kHz). It was shown that, in most test cases,  $\mathcal{L}(f_m)$  can be described by the upconversion of the HBT's baseband noise. As a result the frequency dependence, of  $\mathcal{L}(f_m)$ , is dictated by the low frequency noise spectrum rather than the upconversion itself. Deviation from pure  $1/f$  frequency dependence found for the HBT's baseband noise at frequencies above 100 Hz resulted in  $d\mathcal{L}(f_m)/d(f_m)$  deviating from about  $-30$  dB/decade rate. Reduced oscillator phase noise at high collector current is attributed to reduced upconversion in the oscillator.

## I. INTRODUCTION

HETEROJUNCTION bipolar transistors (HBT's) have shown excellent performance in microwave circuits [1]–[4]. Their power capability makes them very attractive for power amplifiers and oscillators. Today, microwave and millimeterwave oscillator applications are addressed by GaAs MESFET and Silicon (Si) bipolar junction transistors (BJT's). One of the most important characteristics of an oscillator is its spectral purity. A common measure of spectral purity is the ratio of the noise power in a 1-Hz bandwidth in one noise sideband at an offset frequency,  $f_m$ , from the carrier to the power of the carrier. This measure is called the noise power spectral density and it is represented by  $\mathcal{L}(f_m)$  with units of dBc/Hz. It is generally accepted that Si BJT's display the best phase noise performance (lowest  $\mathcal{L}(f_m)$ ) of all transistor based oscillator's.

YIG tuned oscillators, using Si BJT's, have demonstrated useful operation up to 18 GHz [5] with  $\mathcal{L}$  (20 kHz) measured to be between  $-100$  and  $-105$  dBc/Hz over the entire tuning range of 2–18 GHz. Si BJT's and GaAs MESFET's were compared directly, at 6 GHz, in [6]. The Si BJT DRO had  $\mathcal{L}(f_m) \approx$

$-75$  and  $-100$  dBc/Hz at 1 and 10-kHz offset frequencies, respectively. The MESFET DRO had  $\mathcal{L}(f_m) \approx -67$  and  $-95$  dBc/Hz at the same offset frequencies. The same holds true in the commercial arena where for example, GaAs MESFET and Si BJT based DRO's typically provide  $\mathcal{L}$  (10 kHz)  $\approx -90$  and  $-95$  dBc/Hz, respectively [7]. FET based oscillators are capable of operating at much higher oscillating frequencies. A MMIC HEMT oscillator has been realized at 130 GHz through the use of an InP based material system instead of a GaAs based system [8]. Dielectric resonator stabilized MESFET oscillators in work by [9]–[11] demonstrated that MESFET based oscillators could also provide excellent  $\mathcal{L}(f_m)$  characteristics.

HBT based oscillator circuits have been built using free-running, VCO, and DRO approaches [2], [4], [13]–[17]. Using a free-running design at 37.7 GHz,  $\mathcal{L}$ (100 kHz) =  $-82$  dBc/Hz was obtained by [2]. In [4] a DRO operating at 11.06 GHz achieved  $\mathcal{L}(f_m) = -76$  and  $-102$  dBc/Hz at 1 and 10 kHz, respectively. All of the  $\mathcal{L}(f_m)$  listed above can be approximately compared with scaling. Using the relation of Leeson [18],  $\mathcal{L}(f_m)$  scales with operating frequency by  $\omega_0^2$ . Scaling with respect to offset frequency is a little more difficult. For the case where upconversion of ideal  $1/f$  noise dominates, within the resonator bandwidth,  $\mathcal{L}(f_m)$  varies as  $1/f_m^3$ .

HBT based oscillators are expected to provide better  $\mathcal{L}(f_m)$  performance than FET based circuits due to reduced low frequency noise. The best low frequency noise results have been obtained by Hayama et al [14] who reported  $1/f$  noise corner frequencies of 400 Hz. In order for HBT oscillators to achieve their ultimate performance, a systematic study of the factors which impact the oscillator noise is required. Considerable effort has been expended on the study of MESFET based oscillators [11], [12], [19]–[21] are examples. On the otherhand, HBT based oscillators are relatively new and to date a systematic study of the parameters which contribute to their characteristics has not been carried out. This paper presents the results of the first systematic experimental study of the role of the device baseband noise ( $1/f$  noise), the upconversion coefficient ( $K'_{FM}$ ), and the low frequency base termination in the phase noise spectral density of HBT oscillators. The baseband noise is an inherent device property which, through upconversion, can degrade the spectral purity of the oscillator. On the otherhand,  $K'_{FM}$  is a characteristic of the oscillator circuit and the active device which indicates how sensitive the oscillator is to phase modulation by an external signal. The results of this work show the significance

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of the upconversion of the HBT's baseband noise. Section II presents the theoretical basis and experimental procedure for this work. Starting from a general phase noise relationship, a simplified relation is obtained for the phase noise in terms of just  $K'_{\text{FM}}$ , and the oscillator baseband noise. Section III describes both the HBT and the oscillator studied in this work. Results of phase noise spectral density and single sideband amplitude modulation (SSB-AM) noise measurements as a function of bias, and low frequency base termination are presented in Section IV. The measured  $K'_{\text{FM}}$  of the oscillator used here is compared with the experimental results for other oscillators in Section V. Section VI describes the baseband noise characteristics of the HBT used in the oscillator. The measured  $\mathcal{L}(f_m)$  is compared with that calculated using the measured  $K'_{\text{FM}}$  and device baseband noise in Section VII. Finally, conclusions are presented.

## II. NOISE UPCONVERSION

### A. Theory of Noise Upconversion

In the early work by Leeson [18],  $\mathcal{L}(f_m)$  was expressed heuristically using physical arguments. In this section, the  $\mathcal{L}(f_m)$  is expressed in terms of: 1) the upconversion coefficient,  $K'_{\text{FM}}$ , and 2) the HBT's baseband noise. The analysis, of the oscillator noise, is based on the approach used by Riddle [23]. This approach is used since it provides a means for expressing the  $\mathcal{L}(f_m)$  in terms of circuit and device parameters which is not done using Leeson's approach. It is based on the idea that the oscillator can be represented by a feedback network with additive noise at the input and the oscillator signal is the output

$$(n_i + jn_q)e^{j\omega_0 t} = D(A, \omega, \epsilon)(A_0 + m + j\beta)e^{j\omega_0 t} \quad (1)$$

$n_i$  and  $n_q$  are the in-phase and quadrature components of the additive noise.  $D$  is the inverted transfer function consisting of a real part,  $U$ , and an imaginary part,  $V$ .  $A_0$  is the mean value of the oscillator amplitude.  $\omega_0$  is the mean value of the oscillator frequency,  $\omega$ .  $\epsilon$  represents the bias condition of the active device of the oscillator.  $m$  and  $\beta$  are the amplitude and phase modulation, respectively. For the noise analysis  $D$  is expanded in a Taylor Series (only the first order terms are retained) and (1) can be written as two equations

$$n_i = \left[ U_0 + A_0 \frac{\partial U}{\partial A} + j\Delta\omega \frac{\partial V}{\partial \omega} \right] m + \left[ j\Delta\omega \frac{\partial U}{\partial \omega} \right] \beta + A_0 \Delta\epsilon \frac{\partial U}{\partial \epsilon} \quad (2)$$

$$n_q = \left[ A_0 \frac{\partial V}{\partial A} - j\Delta\omega \frac{\partial U}{\partial \omega} \right] m + \left[ U_0 + j\Delta\omega \frac{\partial V}{\partial \omega} \right] \beta + A_0 \Delta\epsilon \frac{\partial V}{\partial \epsilon}. \quad (3)$$

$U_0$  is a constant term arising from the expansion of  $D$ .  $\Delta\epsilon$  represents the perturbation of the bias which can arise due to bias supply fluctuations or device baseband noise. In this work only baseband noise is considered.

These equations can be put into a convenient matrix equation form

$$\begin{bmatrix} \frac{n_i}{A_0} - \Delta\epsilon \frac{\partial U}{\partial \epsilon} \\ \frac{n_q}{A_0} - \Delta\epsilon \frac{\partial V}{\partial \epsilon} \end{bmatrix} = \begin{bmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{bmatrix} \begin{bmatrix} m \\ \beta \end{bmatrix}. \quad (4)$$

The  $M_{ij}$  terms are the modulation transfer terms.  $M_{11}$  is the amplitude to amplitude conversion, while  $M_{22}$  is the phase to phase conversion. The off-diagonal terms are cross-conversion terms.  $M_{21}$  is the amplitude to phase conversion, while  $M_{12}$  is phase to amplitude conversion. The significance of cross-conversion is affected directly by the oscillator design. It will be minimized when the oscillator stability is maximized.

The oscillator phase and amplitude noise spectral densities,  $S_\phi(\omega_m)$  and  $S_A(\omega_m)$ , respectively, are given by

$$S_\phi(\omega_m) = \overline{\beta^2} \quad (5)$$

$$S_A(\omega_m) = \overline{m^2} \quad (6)$$

where  $\omega_m = \Delta\omega$  is the frequency offset from the carrier.

Several points are demonstrated by these equations: 1) baseband noise contributes to the AM and PM noise; 2) additive noise at the oscillation frequency also contributes directly to the AM and PM noise and 3) AM noise can be converted to PM noise and vice versa. In this work, we are investigating the role of the upconversion of the HBT's baseband noise in the oscillator's PM noise.

In the case where the cross-conversion terms are zero,  $S_\phi(\omega_m)$  is given by

$$S_\phi(\omega_m) = \frac{\left( \frac{n_q}{A_0} \right)^2}{\left( \omega_m \frac{\partial V}{\partial \omega} \right)^2} + \frac{\overline{\Delta\epsilon^2} \left| \frac{\partial V}{\partial \epsilon} \right|^2}{\left( \omega_m \frac{\partial V}{\partial \omega} \right)^2} (\text{Hz}^2/\text{Hz}) \quad (7)$$

where we have made use of the fact that  $U_0 \ll \omega_m \frac{\partial V}{\partial \omega}$  [23]. The first term contributes a  $1/f^2$  component due to the  $\omega_m^2$  term. The second term accounts for the upconversion of the baseband noise ( $\overline{\Delta\epsilon^2(\omega_m)}$ ) and has a  $1/f^3$  dependence if  $\overline{\Delta\epsilon^2(\omega_m)}$  has a  $1/f$  dependence. Since the low frequency noise will have a  $1/f^\alpha$  dependence, it will be more significant than the additive noise component in our measurement range. As a result, we will assume that the second term will be dominant. Therefore, we can write

$$S_\phi(f_m) \approx \frac{\overline{\Delta\epsilon^2(\omega_m)} \left| \frac{\partial V}{\partial \epsilon} \right|^2}{\omega_m^2 \tau_g^2} \quad (8)$$

where we have used  $\tau_g = \left| \frac{\partial V}{\partial \omega} \right|$  [24]. For low level modulation,  $\mathcal{L}(f_m)$  is approximated by

$$\mathcal{L}(f_m) \approx \frac{S_\phi(f_m)}{2} = \frac{\overline{\Delta\epsilon^2(f_m)} \left| \frac{\partial V}{\partial \epsilon} \right|^2}{2\omega_m^2 \tau_g^2} \quad (9)$$

The upconversion coefficient,  $K'_{\text{FM}}$ , is defined as

$$K'_{\text{FM}} = \left| \frac{\partial V}{\partial \epsilon} \right| \frac{1}{2\pi\tau_g} (\text{MHz/V}). \quad (10)$$

So  $\mathcal{L}(f_m)$  is given by

$$\mathcal{L}(f_m) \approx \frac{\overline{\Delta\epsilon^2(f_m)}}{2f_m^2} K_{\text{FM}}'^2. \quad (11)$$

$K'_{\text{FM}}$  quantifies how strongly the low frequency noise,  $\Delta\epsilon^2(f_m)$ , is upconverted. It is a function of both the oscillator circuit and the HBT (through  $\tau_g$  and  $|\frac{\partial V}{\partial \epsilon}|$ ). For the case where  $f_m$  is sufficiently small,  $K'_{\text{FM}}$  can be expressed in terms of the oscillator  $\tau_g = \frac{2Q}{\omega_0}$  [23]

$$K'_{\text{FM}} = \left| \frac{\partial V}{\partial \epsilon} \right| \frac{\omega_0}{4\pi Q}. \quad (12)$$

$\mathcal{L}(f_m)$  results from the low frequency noise perturbing the imaginary part of the oscillator's inverted transfer function as already expressed by (7).

### B. Experimental Procedure for Determining Noise Upconversion

As shown in the Appendix,  $D$  is a complicated expression involving device and resonator parameters. As a consequence,  $K'_{\text{FM}}$  is cumbersome to determine analytically. In this work  $K'_{\text{FM}}$  is determined experimentally. To do so consider a phase modulated signal,  $s(t)$

$$s(t) = A \cos \left[ \omega_0 t + \theta_0 + \frac{K'_{\text{FM}} A_m}{f_m} \sin(\omega_m t) \right] \quad (13)$$

where  $A$  is the signal amplitude,  $\omega_0$  is the carrier frequency,  $A_m$  is the amplitude of the modulating signal, and  $\omega_m$  is the modulating frequency;  $K'_{\text{FM}}$  is also referred to as the conversion efficiency of the modulating signal. The upconversion coefficient is now given by

$$K'_{\text{FM}} = \frac{\gamma f_m}{A_m} \quad (14)$$

where  $\gamma$  is the modulation index. The equivalence of (10) and (14) can be shown by calculating the sideband power to carrier power ratio,  $\mathcal{L}(f_m)$ , for (13) for  $\gamma \leq 0.2$  which gives

$$\mathcal{L}(f_m) \approx \frac{K_{\text{FM}}^2 A_m^2}{4 f_m^2}. \quad (15)$$

Letting  $A_m^2/2 = \overline{\Delta\epsilon^2(f_m)}$  and equating (15) and (9) will give (10). To determine  $K'_{\text{FM}}$ ,  $f_m$  or  $A_m$  is varied until the carrier is suppressed. This evaluation is based on the equation for the modulated signal,  $s(t)$ , which can be expressed in terms of Bessel functions as [25]

$$s(t) = A \{ J_0(\gamma) \cos \omega_0 t + J_1(\gamma) [\cos(\omega_0 + \omega_m)t - \cos(\omega_0 - \omega_m)t] + J_2(\gamma) [\cos(\omega_0 + 2\omega_m)t + \cos(\omega_0 - 2\omega_m)t] \cdots \} \quad (16)$$

where  $J_n(\gamma)$  is the  $n$ th order Bessel function. Using the fact that the carrier is suppressed (i.e.  $J_0(\gamma) = 0$ ) for  $\beta \approx 2.4$ ,  $K'_{\text{FM}}$  can then be calculated from (14). In this work,  $K'_{\text{FM}}$  was determined by superimposing a low frequency voltage on the base and varying the amplitude until the carrier was suppressed.

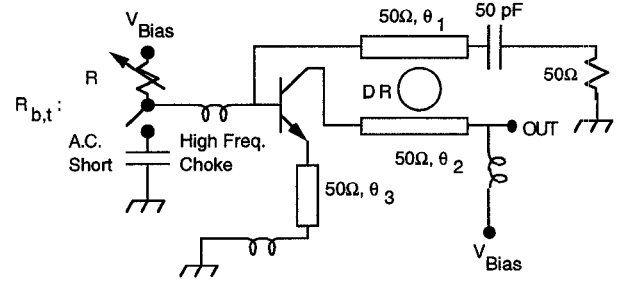


Fig. 1. Schematic diagram of the Dielectric Resonator Oscillator used in this Work.

### III. HBT AND OSCILLATOR DESCRIPTION

The HBT used in these experiments is a *Npn* GaAs/AlGaAs device. It has five emitter fingers  $2 \mu\text{m} \times 20 \mu\text{m}$  giving a total emitter area of  $200 \mu\text{m}^2$ . The devices were fabricated from MOCVD grown material using a self-aligned process which served to minimize parasitic resistances [4]. Their  $f_T$  and  $f_{\text{max}}$  are 20 and 40 GHz, respectively. The oscillator studied in this work is a Dielectric Resonator Oscillator (DRO). Parallel feedback is used with the dielectric resonator providing the necessary inductive feedback between the collector and the base [4]. Series feedback in the emitter circuit is used to improve output matching. A schematic diagram of the DRO is shown in Fig. 1. The collector and base bias are supplied from a single variable DC voltage source which is connected to the circuit through high frequency chokes. The base current is controlled via a 10-KΩ wirewound potentiometer (external to the fixture). The low frequency base termination  $R_{b,t}$  can be switched from  $R$  (the value set by the wirewound potentiometer) to approximately  $0 \Omega$  (the impedance of the shunt capacitor). The high frequency choke allows signal transmission below 100 kHz.

Fig. 2 shows the measured spectrum for the low frequency short circuit base termination case, with  $V_{\text{CE}} = 5 \text{ V}$  and  $I_C = 50 \text{ mA}$ . The oscillation frequency is 11.02 GHz, and the output power was 5.6 dBm. This was verified to be the correct operating mode. No tuning of the emitter stub was attempted to maximize the output power. The output spectrum is clean. Beyond 2 kHz, the spectrum analyzer noise floor dominates the output. The external  $Q$ ,  $Q_{\text{ext}}$ , of the oscillator was measured using the frequency pulling technique described by Kurokawa [22],  $Q_{\text{ext}}$  ranges from approximately 1200 to 2200 as  $I_C$  is decreased from 50 mA to 20 mA.

### IV. PHASE NOISE AND AM NOISE RESULTS

The  $\mathcal{L}(f_m)$  of the DRO was measured from 10 to 100 kHz using an HP3048A phase noise measurement system. Both the bias conditions and the low frequency base termination,  $R_{b,t}$ , were varied.  $V_{\text{CE}}$  was set to either 3 or 5 V, and  $I_C$  was varied from the minimum required to sustain oscillation to 50 mA.  $R_{b,t}$  was set to either the bias resistance,  $R$ , needed for a given  $I_C$ , or  $0 \Omega$  (a.c. short) using a shunt capacitor (external to the test fixture) from the base to ground. The  $R_{b,t}$  was not cooled because its room temperature noise voltage spectral density was calculated to be approximately two orders of magnitude below that measured for the HBT. Fig. 3 is a plot of  $\mathcal{L}(f_m)$

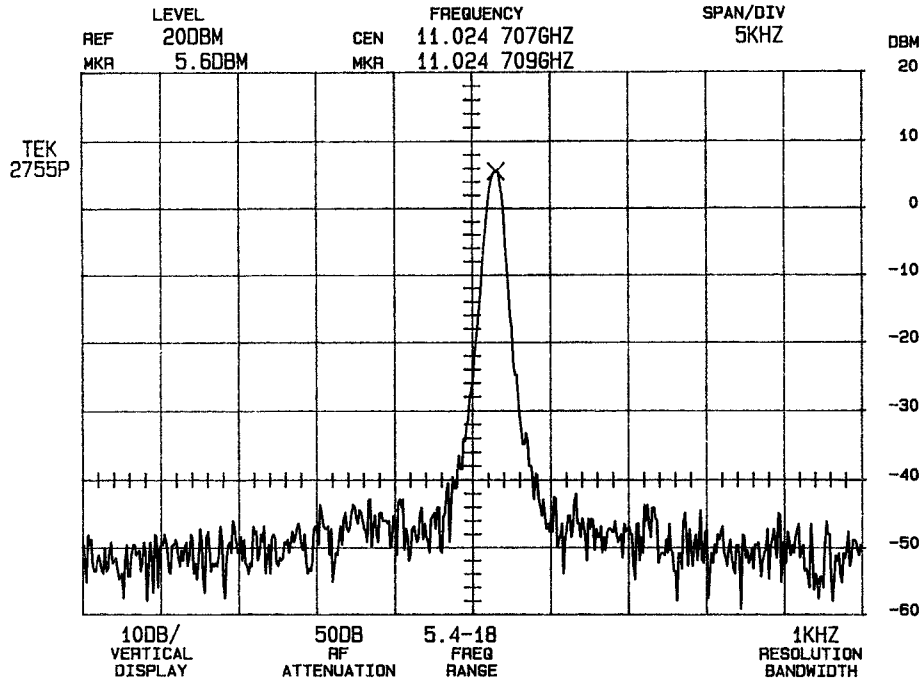


Fig. 2. Measured spectrum of the DRO for  $V_{CE} = 5$  V,  $I_C = 50$  mA, and low frequency short circuit base termination.

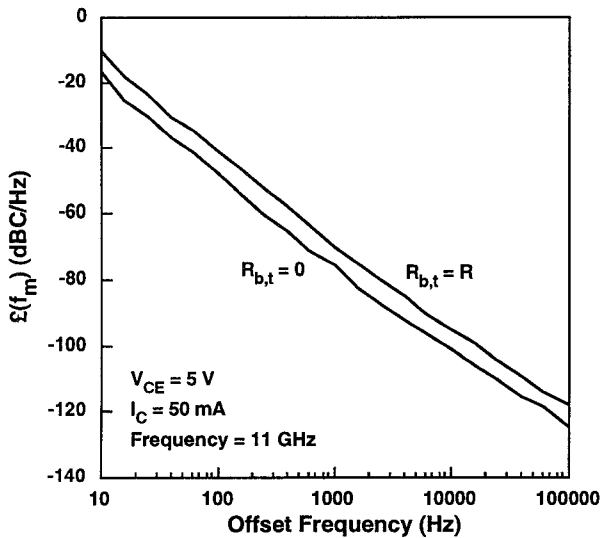


Fig. 3. Comparison of the phase noise,  $\mathcal{L}(f_m)$ , for  $V_{CE} = 5$  V and  $I_C = 50$  mA for different base terminations.

versus frequency for  $V_{CE} = 5$  V,  $I_C = 50$  mA, and two different base termination conditions. This figure clearly shows the impact of the base termination on  $\mathcal{L}(f_m)$ . The noise was reduced by about 4–7 dB over the entire measurement band when the base was a.c. short circuited at baseband frequencies.

The results for  $\mathcal{L}(f_m)$  for various bias conditions and load terminations are summarized in Table I at a 10 kHz-offset. The best result, at a 10-kHz offset, is  $-101$  dBc/Hz for  $V_{CE} = 5$  V,  $I_C = 50$  mA, and  $R_{b,t} = 0$   $\Omega$ . This decreased to  $-124$  dBc/Hz, at a 100-kHz offset using the same bias conditions.  $\mathcal{L}(10 \text{ kHz})$  decreases as  $I_C$  is increased. For instance,  $\mathcal{L}(10 \text{ kHz})$  decreased from  $-94$  dBc/Hz to  $-101$  dBc/Hz as  $I_C$  was increased from 20 to 50 mA with  $V_{CE} = 5$  V and  $R_{b,t} = 0$

TABLE I  
 $\mathcal{L}(10 \text{ kHz})$  OF THE DRO FOR VARIOUS BIAS CONDITIONS AND BASE TERMINATIONS.  $R_{b,t} = R$  IS THE CASE WHEN THE BASE IS TERMINATED INTO THE BIAS RESISTOR  $R_{b,t} = 0$  IS THE CASE WHERE THE BASE IS TERMINATED INTO A SHUNT CAPACITOR

$V_{CE}$ (V)	$I_C$ (mA)	$\mathcal{L}(10\text{kHz})$ (dBc/Hz) $R_{b,t} = R$	$\mathcal{L}(10\text{kHz})$ (dBc/Hz) $R_{b,t} = 0$
3	40	-91	-93
3	50	-93	-97
5	20	-91	-94
5	30	-89	-96
5	40	-92	-99
5	50	-95	-101

$\Omega$ . In addition,  $\mathcal{L}(f_m)$  also decreases with the use of a short circuit base termination. The decrease varied from 2 to 7 dB depending on the bias condition. Moreover,  $\mathcal{L}(f_m)$  decreased as  $V_{CE}$  is increased. For instance, for  $I_C = 50$  mA and  $R_{b,t} = 0$   $\Omega$ ,  $\mathcal{L}(f_m)$  decreased by about 4 dB as  $V_{CE}$  was increased from 3 to 5 V.

As discussed in Section II (7), one expects that the slope of  $\mathcal{L}(f_m)$  versus frequency will follow an ideal  $1/f^3$  relation when the phase noise is entirely due to upconversion of ideal  $1/f$  noise. The  $\mathcal{L}(f_m)$  for the oscillator reported here deviates from the  $1/f^3$  dependence for off set frequencies greater than 400 Hz. Fig. 4 is a plot of the slope of  $\mathcal{L}(f_m)$  as a function of frequency ( $d\mathcal{L}(f_m)/df_m$ ). Between 10 and 100 Hz the slope is about  $-30$  dB/decade. However, this changes to about  $-23$  dB/decade from 10 to 100 kHz. In general, at high frequencies, it was found that the slope varied between approximately  $-20$  dB/decade and  $-25$  dB/decade. This change in slope clearly shows that the measured  $\mathcal{L}(f_m)$  is not simply due to upconversion of an ideal  $1/f$  low frequency noise spectrum.

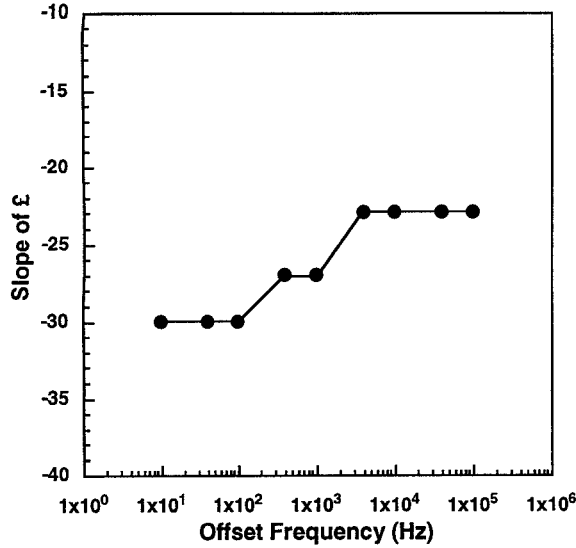


Fig. 4. Slope of oscillator phase noise,  $\mathcal{L}(f_m)$ , showing the deviation from -30 dB/decade.

Typically, one would expect that this change in the slope would be the result of the contribution due to additive noise. As will be seen later, this change might also be at least partially attributed to the HBT's low frequency noise spectra which is not entirely  $1/f$  in nature, but can vary as a function of  $1/f^\alpha$  with  $0.4 \leq \alpha \leq 1.1$ .

SSB-AM noise was measured by feeding the oscillator signal to a system consisting of a detector (Krytar Inc., 0.01–26.5 GHz) followed by a DC block and a preamplifier (North American Aerospace Corp., DC-100 kHz) and an HP3561A signal analyzer. The system noise floor was measured with the oscillator off. This was subtracted from the results measured when the oscillator was on. The difference was assumed to be due to the AM noise of just the oscillator itself. Fig. 5 is a plot of AM noise compared to phase noise. The AM noise is significantly lower than  $\mathcal{L}(f_m)$  over the 10 Hz to 100 kHz measurement band. This low AM noise level is not surprising since the oscillator operates in a saturated amplitude mode. As a result, the amplitude noise is expected to be quite low. Since the  $\mathcal{L}(f_m)$  is clearly the most dominant noise component, this paper concentrates on it and does not deal with the AM noise. In order to begin to understand the  $\mathcal{L}(f_m)$  results, both the baseband noise of the HBT, and the upconversion coefficient,  $K'_{FM}$ , of the oscillator have been characterized and are discussed next.

#### V. MEASUREMENT OF $K'_{FM}$

$K'_{FM}$  was measured for this oscillator as a function of bias and frequency. The results are shown in Fig. 6. Measurements of  $K'_{FM}$  at 5 and 50 kHz showed that it was frequency independent. Similar results have been obtained for measurements made on MESFET's and HEMT's [12]. The bias dependent results showed that  $K'_{FM}$  decreases from 9.2 to 3.2 MHz/V with increasing  $I_C$  (20 to 50 mA,  $V_{CE} = 5$  V). The trend of reduced  $K'_{FM}$  with increased  $I_C$  is consistent with the  $\mathcal{L}(f_m)$  trend with  $I_C$  described by the results in Table I. As will be shown in Section VI an increased  $I_C$  can sometimes result

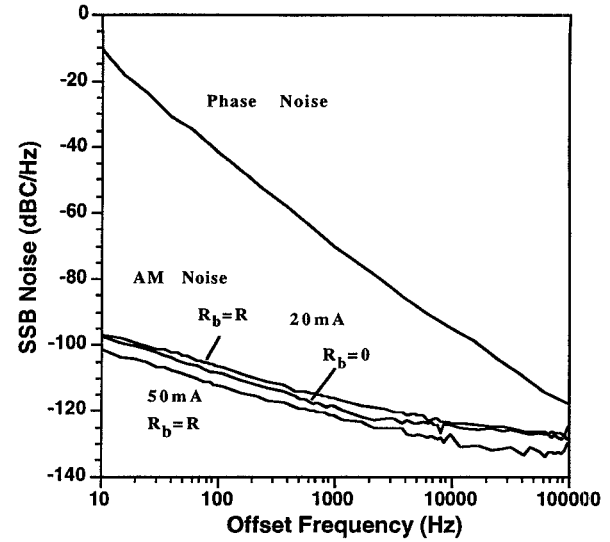


Fig. 5. Comparison of AM noise and  $\mathcal{L}(f_m)$ . The AM noise is shown for  $I_C = 20$  mA with  $R_{b,t} = 0$  and  $R$ ,  $I_C = 50$  mA with  $R_{b,t} = R$ . The  $\mathcal{L}(f_m)$  curve corresponds to  $I_C = 50$  mA with  $R_{b,t} = R$ .

in increased baseband noise for the HBT. Thus the reduced oscillator noise at higher  $I_C$  will be primarily attributed to reduced upconversion in the oscillator. Measurements of  $Q$  indicate that it decreases with increasing  $I_C$  (see Section III). Recalling (12) this would cause  $K'_{FM}$  to increase with  $I_C$ . The  $\frac{\partial V}{\partial \epsilon}$  term represents sensitivity to bias fluctuations. Since following the results of Fig. 6,  $K'_{FM}$  decreases with increasing bias,  $\frac{\partial V}{\partial \epsilon}$  must be responsible for the decrease by also decreasing. Hence, the upconversion coefficient is reduced due to reduction in sensitivity to bias fluctuations. Although one expects the current and voltage to grow to some self-limiting condition when the device is oscillating, regardless of bias, this does not translate to insensitivity of noise to bias conditions. As stated already,  $\frac{\partial V}{\partial \epsilon}$ , and thus the sensitivity of upconversion and noise to bias fluctuations is indeed dependent on the bias.  $K'_{FM}$  showed less sensitivity to  $V_{CE}$ , changing from 3.2 to 2.2 MHz/V while varying  $V_{CE}$  from 5 to 3 V. To the authors' knowledge this resembles the behavior of MESFET oscillators where there is a very small variation with drain-source voltage.

It is interesting to compare the values of  $K'_{FM}$  obtained in this work with those measured for FET based oscillators. In the paper by Rhodin *et al.* [11],  $K'_{FM}$  ranged from 47 to 85 MHz/V when microstrip elements were used.  $K'_{FM}$  was reduced to about 1 MHz/V when dielectric resonator stabilization was used. This reflects the low- $Q$  characteristics of the microstrip components. In [10] and [31] various DRO configurations were used with  $K'_{FM}$  ranging from 0.6 to 3 MHz/V. Free running oscillators had  $K'_{FM}$  of 140 MHz/V in the same work.

The  $|\frac{\partial V}{\partial \epsilon}|$  term of  $K'_{FM}$  arises because the equivalent circuit parameters of the HBT are bias dependent and their perturbation, caused by the bias fluctuations, result in the upconversion of the baseband noise. To study the sensitivity of  $V$  to the HBT's equivalent circuit parameters,  $D$  was derived in terms of the oscillator's equivalent circuit parameters. The equivalent circuit analyzed is shown in Fig. 7 and the equivalent circuit values, which satisfy the oscillation conditions at 10 GHz, are

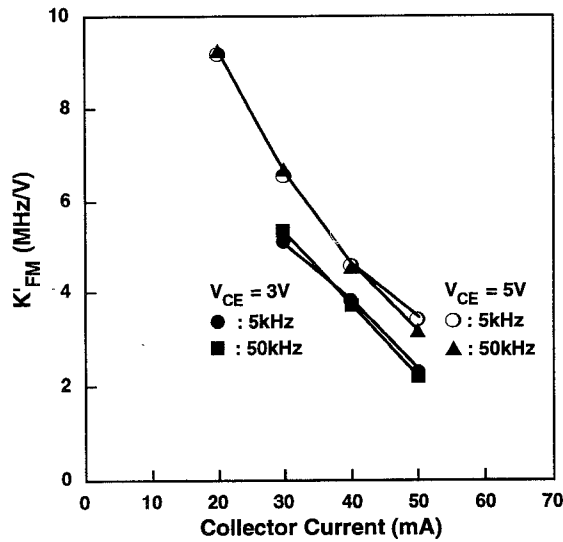


Fig. 6. The upconversion coefficient,  $K'_{FM}$ , as a function of bias and frequency.

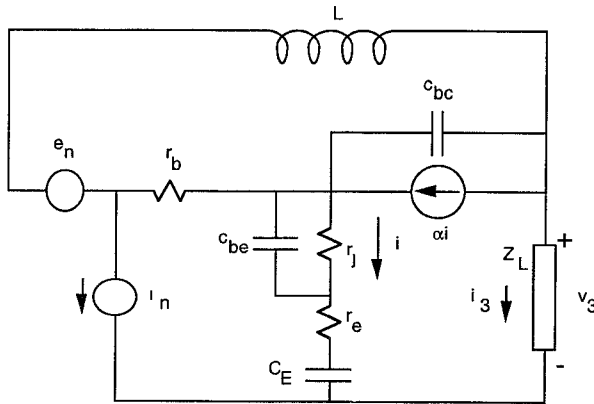


Fig. 7. Equivalent circuit used for calculating the inverted transfer function. The equivalent circuit is based on the Dielectric Resonator Oscillator shown in Fig. 1. Two additive noise sources are included.  $\alpha$  is given by  $\alpha = \alpha_0 \frac{e^{-j\omega\tau}}{1 + j\frac{\omega}{\omega_0}}$ .

in Table II. The additive noise is represented by the general case of a series noise voltage source,  $e_n$ , and a shunt noise current source,  $i_n$ . The presence of the two sources necessitates two different expressions for  $D$ . To simplify the present analysis we have ignored the correlation between the sources.  $D_{i_n}$  is the inverted transfer function derived for the noise current source.  $D_{e_n}$  is the inverted transfer function derived for the noise voltage source. The expressions for  $D_{i_n}$  and  $D_{e_n}$  are given in the Appendix. In order to determine the sensitivity of  $V$  (the imaginary part of  $D$ ) to the equivalent circuit parameters,  $D_{i_n}$  and  $D_{e_n}$  were numerically differentiated with respect to each of the nonlinear circuit elements. For example, the numerical derivative of  $D_{e_n}$  with respect to  $c_{bc}$  was evaluated using

$$\frac{\Delta D_{e_n}}{\Delta c_{bc}} = \frac{D_{e_n0} - D_{e_n1}}{c_{bc} - c'_{bc}} \quad (17)$$

where  $c'_{bc}$  is  $c_{bc}$  reduced by one percent.  $D_{e_n0}$  is the value of the transfer function for the value of the parameters in Table II,  $D_{e_n1}$  is the value of the transfer function when

TABLE II  
VALUES OF THE EQUIVALENT CIRCUIT PARAMETERS USED IN THE CALCULATIONS OF THE INVERTED TRANSFER FUNCTIONS

Circuit Element	Value
$r_b(\Omega)$	6.5
$r_j(\Omega)$	0.5
$c_{be}(pF)$	0.8
$c_{bc}(pF)$	0.141
$\alpha_0$	0.945
$\omega_0(rad/sec)$	$1.26 \times 10^{11}$
$\tau(psec)$	2.0
$C_E(pF)$	0.175
$L(nH)$	1.2
$Z_L(\Omega)$	$84.03 - j0.854$

TABLE III  
SENSITIVITY OF THE IMAGINARY PART OF THE INVERTED TRANSFER FUNCTIONS,  $D_{e_n}$  AND  $D_{i_n}$ , TO THE BIAS DEPENDENT EQUIVALENT CIRCUIT PARAMETERS AT 10GHz.  $r_j$ ,  $c_{be}$ ,  $c_{bc}$ , AND  $\alpha_0$  WERE CONSIDERED. THE GREATEST SENSITIVITY OCCURS FOR  $c_{bc}$

	$\frac{\Delta V}{\Delta \alpha_0}$	$\frac{\Delta V}{\Delta r_j}(\Omega^{-1})$	$\frac{\Delta V}{\Delta c_{be}}(F^{-1})$	$\frac{\Delta V}{\Delta c_{bc}}(F^{-1})$
$D_{in}$	$-2.7 \times 10^{-1}$	$3.6 \times 10^{-3}$	$2.8 \times 10^7$	$-5.8 \times 10^{12}$
$D_{en}$	$6.3 \times 10^{-1}$	$-5.3 \times 10^{-3}$	$6.2 \times 10^7$	$-5.5 \times 10^{12}$

$c_{bc}$  is replaced by  $c'_{bc}$ . The imaginary parts of the derivatives will indicate how sensitive  $V$  is to the circuit elements. The nonlinear elements that were considered are:  $r_j$ ,  $c_{be}$ ,  $c_{bc}$ , and  $\alpha_0$ . Table III summarizes the results at 10 GHz. The greatest sensitivity is to the device capacitances  $c_{bc}$  and  $c_{be}$  where values of approximately  $10^{12}/F$  and  $10^7/F$ , respectively, were obtained. The smallest sensitivity is for  $r_j$  which is approximately  $10^{-3}/\Omega$ .

## VI. HBT LOW FREQUENCY NOISE CHARACTERISTICS

HBT low frequency noise, or baseband noise, can have many origins including: recombination, diffusion, trap, burst, and partition. Moreover, the physical location within the device can vary as well [26]. The work done on the low frequency noise characteristics of HBT's is quite limited in comparison to that done for Si BJT's. Early work dealt with double heterojunction bipolar transistors (DHBT's). The results of this work identified the presence of both  $1/f$  noise and burst noise in the device. The corner frequencies were beyond 100 kHz. The work by [26] dealt with both the short circuit base and collector noise and found that the noise characteristics of these two ports were different. The work by [27] dealt with the excess white noise found in their HBT's. The excess noise turned out to be a single spectral component described by

$$S(\omega) = \frac{\tau}{1 + (\omega\tau)^2} \quad (18)$$

where  $\omega$  is the radian frequency, and  $\tau$  is the time constant of the noise mechanism. Such a component is referred to as a Lorentz component. Tutt *et al.* [28], [29], dealt with

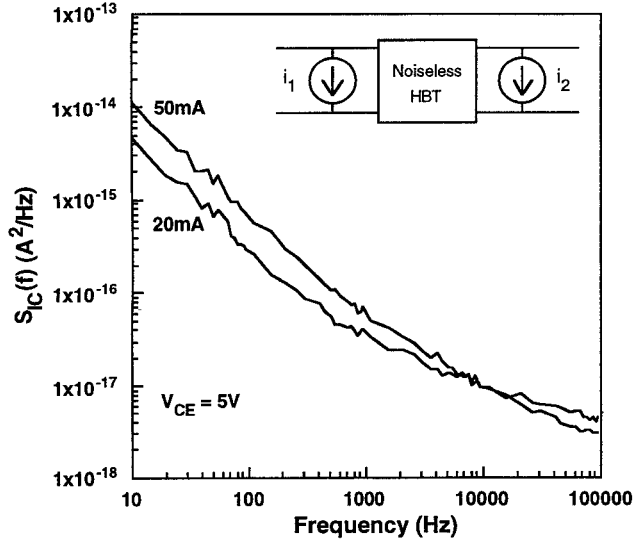


Fig. 8. Low frequency short circuit collector noise spectra,  $S_{I_C}(f)$  as a function of bias and frequency for the HBT used in the oscillator. The inset contains the noise equivalent circuit used for HBT noise characterization.

power HBT structures and observed recombination effects and significant Lorentz components. The Lorentz components were due to traps with an  $E_a$  of about 0.16 and 0.58 eV. The results also indicated saturation effects in the measured  $1/f$  noise. Costa *et al.* [30], investigated bias and temperature dependences, surface passivation effects, the influence of the AlGaAs layer composition, and geometry effects.

Measurement of the noise spectra as a function of bias, frequency, and provides information about the origin(s) of the noise. The inset of Fig. 8 shows the noise equivalent circuit representation that is used. This model is used because the analysis of bipolar transistor noise is done in terms of noise currents. Referring to the inset,  $i_1$  is the short circuit base noise current, with the collector terminal simultaneously short circuited. Its spectra is designated by  $S_{I_B}(f)$  ( $A^2/Hz$ ).  $i_2$  is the short circuit collector noise current, with the base terminal simultaneously short circuited. Its spectra is designated by  $S_{I_C}(f)$  ( $A^2/Hz$ ). Even though one might expect a great deal of similarity between Si BJT's and GaAs/AlGaAs HBT's there is evidence that their noise mechanisms can be different. For instance,  $S_{I_B}(f) = S_{I_C}(f)$  for Si BJT's [10] while  $S_{I_B}(f) < S_{I_C}(f)$  for AlGaAs/GaAs HBT's [28].

Fig. 8 is a plot of  $S_{I_C}(f)$  for  $V_{CE} = 5$  V and  $I_C = 20$  and 50 mA for the device used in the oscillator when it is in a nonoscillating mode. The measurements covered the 10 Hz to 100 kHz frequency range. The noise increased with  $I_C$  in the region which is approximately  $1/f$  in nature ( $S_{I_C}(f)$  increased 3.8 dB at 10 Hz) but, it decreased in the region where the spectra begin to flatten out ( $S_{I_C}(f)$  decreased 1.7 dB at 100 kHz). The bias dependence of the  $1/f$  noise spectra has been determined by measuring  $S_{I_C}(f)$  for various  $I_C$ , and it is found to follow  $S_{I_C}(10 \text{ Hz}) \propto I_C^{1.7}$ . This bias dependence suggests that recombination noise contributes to  $S_{I_C}(10 \text{ Hz})$ . In general, the dependence of  $S_{I_C}(f)$  on  $V_{CE}$  is weak.

The frequency dependence of  $S_{I_C}(f)$  is clearly not  $1/f$  over the entire measurement band. Npn GaAs/AlGaAs HBT's often do not display perfect  $1/f$  noise spectra. It is known

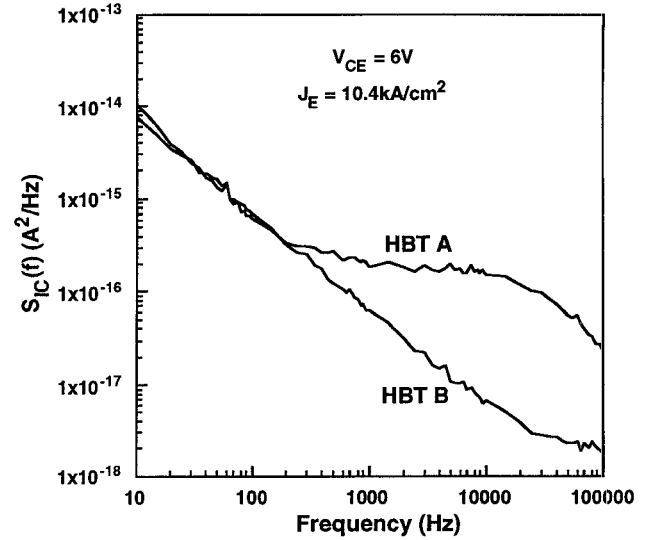


Fig. 9. Comparison of the low frequency noise spectra of two HBT's differing only in their layer design.

that a substantial noise bulge is seen in the  $1/f$  noise spectra [28] in the vicinity of 10 kHz due to trapping. This is often associated with the  $n$ -type doping of the AlGaAs in the emitter and was present in the spectrum of the transistor tested here. As shown in Fig. 8, from 10 to 100 Hz the noise is essentially  $1/f$  in nature. At higher frequencies this tends to reduce dramatically. For example, at frequencies greater than 10 kHz, it decreases to  $1/f^{0.4}$  at  $I_C = 20$  mA, or  $1/f^{0.5}$  at  $I_C = 50$  mA. This is likely due to traps which introduce a Lorentz component to the spectrum. This component will change the frequency dependence of the low frequency noise.

The actual spectral shape can vary widely among Npn GaAs/AlGaAs HBT's as shown in Fig. 9. This figure shows the spectra for two HBT's fabricated with the same process and having identical geometry, but different layer designs. One device clearly demonstrates a Lorentz component between 300 Hz and 100 kHz, while the other does not. The Lorentz component is large enough to cause the spectrum to essentially flatten out (i.e.  $1/f^0$ ) from 1 to 10 kHz. Considering that nonlinear effects are present in the operation of an oscillator, these results indicate that the choice of HBT can impact the phase noise performance.

Up to this point, measurement of the collector noise spectra has assumed that the base was AC short circuited. For the general case where the base can have any termination, we denote the collector noise current spectra by  $S'_{I_C}(f)$ . To determine the impact of the base termination on the measured collector noise,  $S'_{I_C}(f)$  was measured for the base termination used in the oscillator. Fig. 10 shows the measured low frequency noise spectra for the oscillator bias condition  $V_{CE} = 5$  V and  $I_C = 50$  mA. A clear increase of the  $S'_{I_C}(f)$  for the nonzero  $R_{b,t}$  case is shown. At 10 Hz the noise increased by 7.1 dB, while at 100 kHz it increased by 12.4 dB. This effect is easily understood by recalling the noise equivalent circuit of the HBT in Fig. 8. For the short circuit base condition,  $i_1$  has no effect on the total output noise current,  $i_{out}$ . So  $i_{out}^2 = i_2^2$ . This is due to  $i_1$  being shunted out of the device. However, when the base termination is nonzero, some fraction,  $k$ , of  $i_1$  flows into the

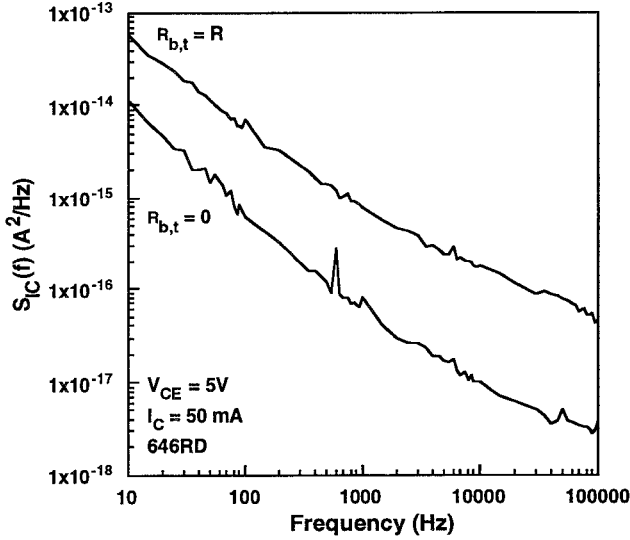


Fig. 10. Impact of the low frequency base termination on the output noise spectra.

base where it is then amplified, by  $h_{fe}$ , and contributes to the total output noise current. Since  $i_1$  and  $i_2$  may be correlated,  $i_{out}$  becomes

$$\overline{i_{out}^2} = \overline{(kh_{fe}i_1 + i_2)^2} = (kh_{fe})^2\overline{i_1^2} + \overline{i_2^2} + 2ckh_{fe}\sqrt{\overline{i_1^2} \cdot \overline{i_2^2}} \quad (19)$$

where  $c = \frac{\overline{i_1 i_2}}{\sqrt{\overline{i_1^2} \cdot \overline{i_2^2}}}$  is the correlation coefficient. The resulting amplitude of the output noise is affected by the correlation, input termination, magnitude of the input noise spectra, and gain of the device. For devices used in this work, a resistive base termination resulted in an increased noise at the output. In all of the measurements carried out, the corner frequency was never found to be below 100 kHz. This is consistent with the results of Costa [30].

The HBT baseband noise has been presented in terms of noise current spectral density, however, in the previous section the upconversion coefficient is given in units of MHz/V. In order to use the measured baseband noise it must be transformed into an equivalent input noise voltage spectral density,  $S_{IV}(f)$  ( $V^2/Hz$ ). The equivalent input noise voltage is obtained using

$$S_{IV}(f) = \frac{S_{IC}(f)R_L^2}{A_V^2(f)} = \frac{S_{IC}(f)}{g_m^2(f)} \quad (20)$$

where  $R_L$  is the collector load resistor used for the baseband noise measurement and  $A_V(f)$  is the voltage gain of the HBT in the test circuit. Fig. 11 is a plot of  $S_{IV}(f)$  for the HBT measured for  $I_C = 20$  mA and 50 mA with the base terminated into either  $R \Omega$  or approximately  $0 \Omega$ . For the case where the base is terminated into  $0 \Omega$  the  $S_{IV}(f)$  spectra are equal at low frequencies. As the frequency increases the noise at 50 mA is less than that at 20 mA. In fact, the  $S_{IV}$  (100 kHz), for the 50 mA case, is almost 5 dB less. This occurs because the voltage gain is greater for the 50 mA case ( $A_v$  (100 kHz) = 6.1) compared to the 20 mA case ( $A_v$  (100 kHz) = 4.0) and, as shown in Fig. 8, the  $S_{IC}$  (100 kHz) is approximately

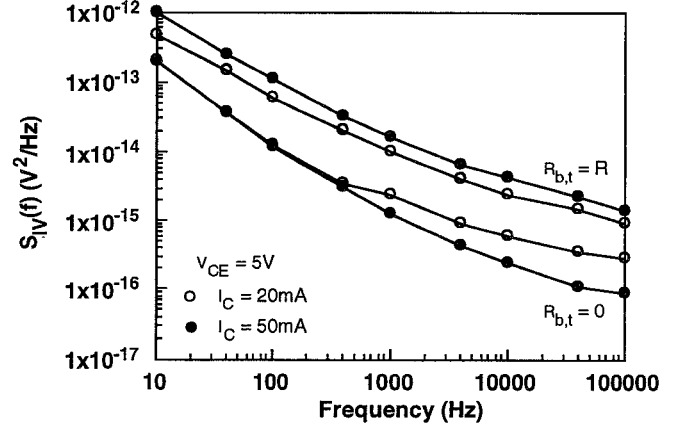


Fig. 11. Equivalent input noise voltage spectra for the HBT used in the DRO. The measured spectra correspond to  $I_C = 20$  and 50 mA with the base terminated into  $R \Omega$  and  $0 \Omega$ .

1.7 dB lower for the 50-mA case. For the case where the base is terminated into  $R \Omega$  the  $S_{IV}(f)$  is approximately 2 dB greater for the 50-mA case over the entire frequency range. This is due to the fact that the base noise current of the HBT increases with bias [29] which, through (19) and (11), results in an effectively larger  $S_{IV}(f)$ .

It is useful to compare the  $S_{IV}(f)$  of HBT's and MESFET's, however, the appropriate normalization must be used.  $S_{IV}(f)$  of MESFET's is normalized to the gate width according to Graffeuil [10]. The MESFET's used in the work by Camiade *et al.* [31] had  $S_{IV}(10 \text{ kHz})$  ranging from  $3.33 \times 10^{-18} \text{ V}^2/\text{Hz}/\mu\text{m}$  to  $133 \times 10^{-18} \text{ V}^2/\text{Hz}/\mu\text{m}$ . The correct normalization for the HBT noise depends on the origin of the noise. Test structures were not available to determine if  $S_{IC}$  was either periphery or area dependent, consequently, it was normalized to the emitter width. Since  $g_m$  is also proportional to the emitter width,  $S_{IV}$  is inversely proportional to the emitter width through (20). The HBT here had  $S_{IV}(10 \text{ kHz}) = 2.4 \times 10^{-18} \text{ V}^2/\text{Hz}/\mu\text{m}$  for the best  $\mathcal{L}(f_m)$  case ( $I_C = 50$  mA and  $R_{b,t} = 0$ ). This is comparable to the lowest values of the MESFET's.

## VII. CALCULATION OF $\mathcal{L}(f_m)$ USING $K'_{FM}$ AND DEVICE BASEBAND NOISE

Using the experimentally determined values of  $K'_{FM}$  and  $S_{IV}(f)$ , the phase noise, due to upconversion of baseband noise, can be calculated using  $10 \log[\mathcal{L}(f_m)]$  of (15).  $A_m^2/2$  is replaced by the equivalent input noise voltage spectral density,  $S_{IV}(f)$ , of the HBT. This assumes that the device noise, measured in a nonoscillating condition, is valid for the oscillating condition. Fig. 12(a) and (b) contain measured and calculated  $\mathcal{L}(f_m)$  for  $V_{CE} = 5$  V and  $I_C = 20$  mA for  $R_{b,t} = 0 \Omega$  and  $R$ . The agreement in both cases is very good, typically less than 3-dB difference. This shows that the  $\mathcal{L}(f_m)$  can be described by the upconversion of the device's baseband noise.

Measured and calculated  $\mathcal{L}(f_m)$  were also compared for the cases of  $V_{CE} = 5$  V and  $I_C = 50$  mA with  $R_{b,t} = 0 \Omega$  and  $R$  [Fig. 13(a) and (b)]. In the case of  $R_{b,t} = R$  the agreement is again very good showing that  $\mathcal{L}(f_m)$  can be described by



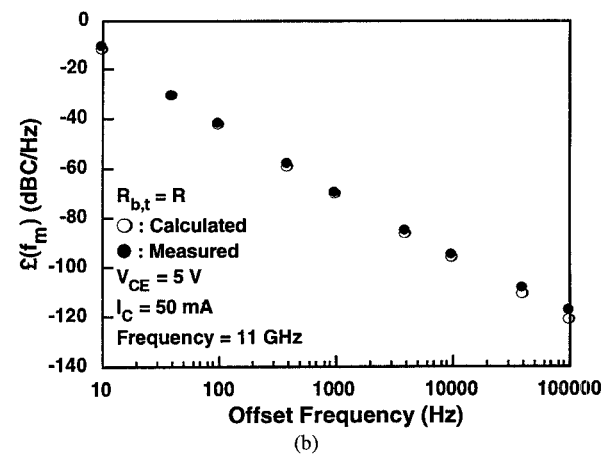
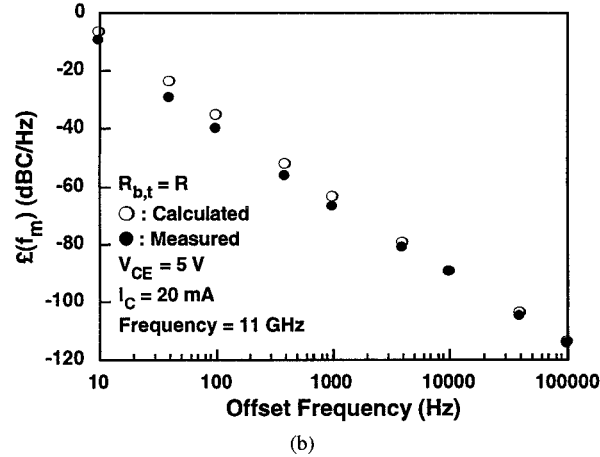
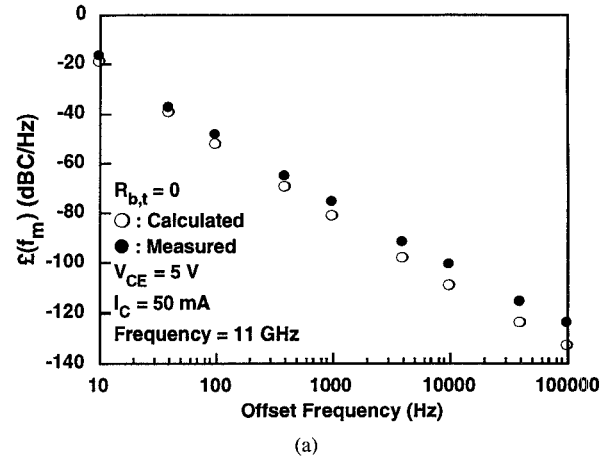
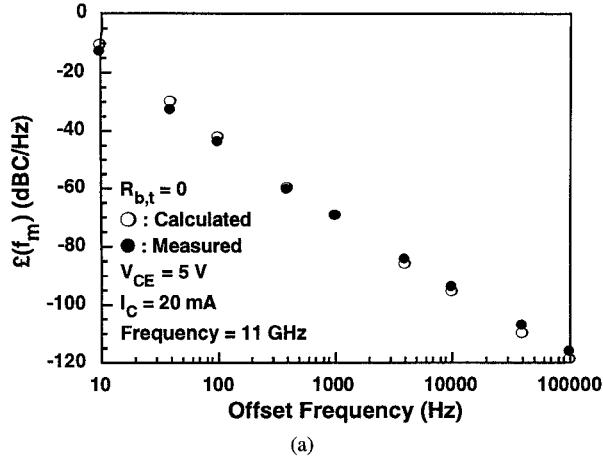


Fig. 12. Comparison of calculated and measured  $\mathcal{L}(f_m)$  for  $V_{CE} = 5$  V and  $I_C = 20$  mA. These results are for  $R_{b,t} = 0$  and  $R$  base terminations.

Fig. 13. Comparison of calculated and measured  $\mathcal{L}(f_m)$  for  $V_{CE} = 5$  V and  $I_C = 50$  mA. These results are for  $R_{b,t} = 0$  and  $R$  base terminations.

the upconversion of the device's baseband noise. In contrast, for the case of  $R_{b,t} = 0$   $\Omega$ , the agreement is good at very low offset frequencies, however, an increasing discrepancy occurs at higher frequencies. The discrepancy is as great as 9 dB at 100 kHz. This indicates, for this case,  $\mathcal{L}(f_m)$  is not simply due to upconverted baseband noise. Recalling (2), the complete oscillator noise description requires the modulation conversion matrix. There are three sources of phase noise: 1) additive noise at the operating frequency, 2) upconverted baseband noise and 3) AM-PM conversion. In the case of  $R_{b,t} = 0$ , the upconverted baseband noise is not dominant and one, or both, of the other two sources dominates. In the  $R_{b,t} = R$  case, the equivalent input noise voltage,  $S_{IV}(f)$ , is larger. Since the oscillator is operating in a saturated amplitude mode this will not affect the AM-PM contribution. Moreover, the additive noise contribution is not affected either. Agreement of theory and experiment is therefore better since the only significant noise mechanism present is baseband noise upconversion; (11) used for the theoretical prediction accounts only for noise upconversion and consequently predict better the oscillator performance in such cases.

Comparing the trends observed for  $K'_{FM}$  (Fig. 6) and for  $S_{IV}(f)$  (Fig. 11) with those of  $\mathcal{L}(f_m)$ , the increase in  $\mathcal{L}(f_m)$  with  $R_{b,t} = R$  is entirely due to the increased  $S_{IV}(f)$ . The bias dependence of  $\mathcal{L}(f_m)$ , however, cannot be explained in terms of the bias dependence of  $S_{IV}(f)$ . For instance, increasing  $I_C$

from 20 to 50 mA, with  $R_{b,t} = R$ , results in a 2.4-dB increase in  $S_{IV}$  (10 kHz), while  $\mathcal{L}(10$  kHz) decreases approximately 4 dB. The bias dependence of  $\mathcal{L}(10$  kHz) is therefore dominated by that of  $K'_{FM}$  which decreases with increasing  $I_C$ . On the other hand, the frequency dependence of  $\mathcal{L}(f_m)$  is determined by the baseband noise and not  $K'_{FM}$  which was shown to be frequency independent.

## VIII. CONCLUSION

The  $\mathcal{L}(f_m)$  and AM noise of a HBT DRO have been measured as a function of bias and low frequency base termination. The SSB-AM noise is far less than  $\mathcal{L}(f_m)$ . Best  $\mathcal{L}(f_m)$  obtained was  $-124$  dBc/Hz at a 100 kHz offset at  $V_{CE} = 5$  V,  $I_C = 50$  mA, and a short circuit base termination.  $\mathcal{L}(f_m)$  decreased by as much as 7 dB (at a 10-kHz offset frequency) by increasing  $I_C$ , from 20 to 50 mA. In addition,  $\mathcal{L}(f_m)$  also decreased by as much as 7 dB (at a 10-kHz offset frequency) through the use of a short circuit low frequency base termination due to shunting the base noise of the transistor. The roles of the upconversion coefficient,  $K'_{FM}$ , and the HBT's baseband noise in  $\mathcal{L}(f_m)$  were studied.  $K'_{FM}$  decreases with increasing  $I_C$  which is consistent with  $\mathcal{L}(f_m)$ . On the other hand, the baseband noise tended to increase slightly with increasing  $I_C$ . In most cases measured  $\mathcal{L}(f_m)$  could be modeled using the HBT's baseband noise and,  $K'_{FM}$ , with agreement typically within 3 dB. Under some conditions either cross-modulation or additive noise may

$$D_{i_n} = \frac{i_n}{v_3 Y_L} \quad (21)$$

$$= \frac{[Y_2(\alpha Y_E - Y_2) + (Y_L + Y_1 + Y_2)(g_b + Y_2 + Y_E(1 - \alpha))](g_b + Y_1)}{Y_L[Y_1(g_b + Y_2 + Y_E(1 - \alpha)) - g_b[\alpha Y_E - Y_2]]} - \frac{[Y_1 Y_2 + g_b(Y_L + Y_1 + Y_2)]g_b}{Y_L[Y_1(g_b + Y_2 + Y_E(1 - \alpha)) - g_b[\alpha Y_E - Y_2]]} - \frac{Y_1}{Y_L} \quad (22)$$

become more significant. Modeling  $\mathcal{L}(f_m)$  using  $K'_{FM}$  and the baseband noise shows that the frequency dependence of  $\mathcal{L}(f_m)$  is governed by the frequency dependence of the baseband noise since  $K'_{FM}$  is frequency independent.

#### APPENDIX

##### TRANSFER FUNCTION FOR THE DRO

The oscillator used in this study was a dielectric resonator oscillator with feedback between the collector and the base (Fig. 1). The small signal equivalent circuit of the oscillator is shown in Fig. 7. The additive noise sources,  $e_n$  and  $i_n$  are included as well. Since there are two additive noise sources there are two transfer functions  $D_{i_n}$  and  $D_{e_n}$  for  $i_n$  and  $e_n$ , respectively. Equations (21) and (22) are shown at the top of this page, where

$$\begin{aligned} Y_1 &= \frac{1}{j\omega L} \\ Y_2 &= j\omega C_{bc} \\ Y_E &= \left[ r_E + \frac{r_j}{1 + j\omega C_{be} r_j} + \frac{1}{j\omega C_E} \right]^{-1} \\ g_b &= \frac{1}{r_b} \\ Y_L &= \frac{1}{Z_L}. \end{aligned} \quad (23)$$

$Y_L$  is the total load admittance, and  $v_3$  is the voltage across  $Y_L$ . In this analysis the effect of the DRO is approximated by a lumped element inductor,  $L$ .

$$\begin{aligned} D_{e_n} &= \frac{e_n}{i_3 Z_L} \\ &= - \left[ \frac{Z_2(1 - \alpha)(r_b + Z_1) + (Z_E + Z_L)(r_b + Z_1 + Z_2)}{Z_2 Z_L} \right] \end{aligned} \quad (24)$$

(25)

where

$$\begin{aligned} Z_1 &= j\omega L \\ Z_2 &= \frac{1}{j\omega C_{bc}} \\ Z_E &= \left[ r_E + \frac{r_j}{1 + j\omega C_{be} r_j} + \frac{1}{j\omega C_E} \right]. \end{aligned} \quad (26)$$

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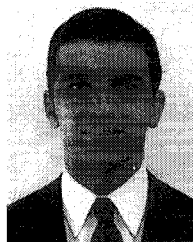
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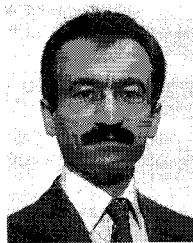
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